

PART I MPT [Markowitz]

1. ER & S.D.

Single stock

- Ex post data

$$ER = \frac{\sum x}{n}$$

$$\sigma_x = \sqrt{\frac{\sum (x - \bar{x})^2}{n}}$$

- Ex-Ante data

$$ER = \sum p x$$

$$\sigma_x = \sqrt{\sum (x - \bar{x})^2 p}$$

- C.V. = $\frac{\sigma}{\bar{x}}$

2. Covariance & Correlation

• Cov_{xy}

- Ex post data

$$Cov_{xy} = \frac{\sum (x - \bar{x})(y - \bar{y})}{n}$$

- Ex Ante data

$$Cov_{xy} = \sum (x - \bar{x})(y - \bar{y}) p$$

$$\rho_{xy} = \frac{Cov_{xy}}{\sigma_x \sigma_y}$$

Concept

1. $\rho_{xy} = +1$

Risk can't be reduced

$$\sigma_p = (\sigma_x \times \omega_x) + (\sigma_y \times \omega_y)$$

2. $\rho_{xy} = -1$

Zero Risk portfolio

$$\omega_A = \frac{\sigma_B}{\sigma_A + \sigma_B}$$

$$\sigma_p = \sqrt{\sigma_A^2 \omega_A^2 + \sigma_B^2 \omega_B^2 + 2 \times \sigma_A \times \omega_A \times \sigma_B \times \omega_B \times \rho_{AB}}$$

3. $\rho_{xy} = \text{other}$

Minimum Risk portfolio

$$\omega_A = \frac{\sigma_B^2 - Cov_{AB}}{\sigma_A^2 + \sigma_B^2 - 2Cov_{AB}}$$

Sharpe Ratio

$$SR = \frac{ER - R_f}{\sigma_p}$$

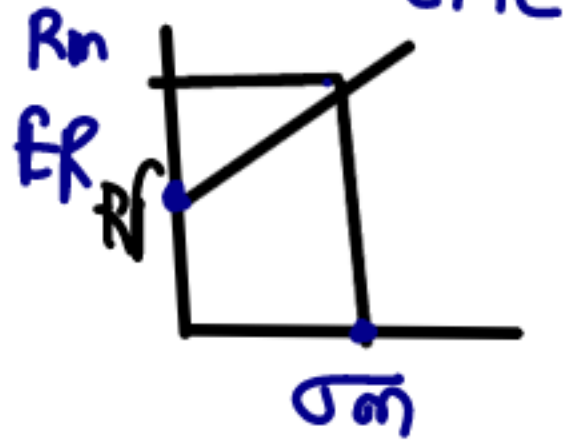
PART II CAPM

Capital Market Theory

$$ER_p = R_f + \left(\frac{R_m - R_f}{\sigma_m}\right) \sigma_p$$

$$\sigma_p = \sigma_m \times w_m$$

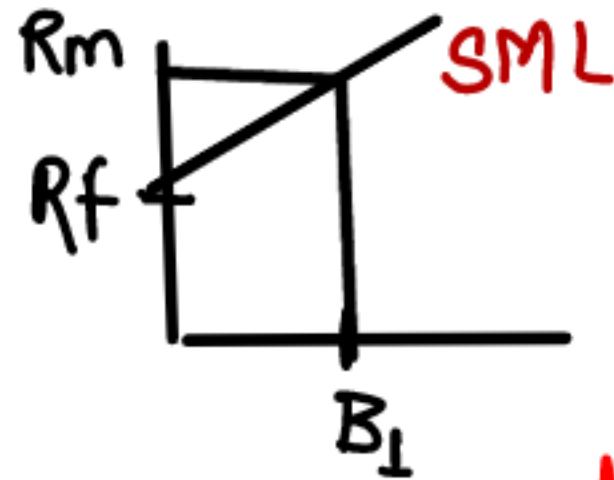
[Market & Rf]
CML



① Equation

$$ER = R_f + (R_m - R_f) \beta$$

- SR = Market Related
- UR = Specific Risk



② Beta calculation

$$i) \beta = \frac{\Delta \text{Stock Return}}{\Delta \text{Market Return}}$$

$$ii) \beta = \frac{\sigma_x}{\sigma_y} \times r_{xy}$$

$$iii) \beta = \frac{COV_{xy}}{\sigma_m^2}$$

$$iv) \beta = \frac{\sum x_m - n \bar{x} \bar{m}}{\sum m^2 - n \bar{m}^2}$$

③ Beta Management

$B_p = \text{Weighted Avg}$

- Using Rf
- $WA = \frac{B_T}{B_P}$
- Using other stock

④ Alpha

$$\text{Alpha} = ER - K_e$$

positive → Buy
negative → Sell

⑤ Asset pricing

$$P_0 = \frac{D_1}{K_e - g}$$

Actual price > P_0 - Sell
Actual price < P_0 - Buy

⑥ TR, SR & UR

• Single Stock

$$TR = \sigma_x^2$$

$$SR = \beta^2 \sigma_m^2$$

$$\sigma_{ex}^2 = TR - SR$$

$$r^2 = \frac{SR}{TR} \text{ (coefficient of determination)}$$

• PORTFOLIO

$$\bullet SR_p = \beta_p^2 \sigma_m^2$$

$$\bullet \sigma_{ep}^2 = \textcircled{1} TR_p - SR_p$$

$$\textcircled{2} \sigma_A^2 \omega_A^2 + \sigma_B^2 \omega_B^2$$

$$\bullet TR_p = \sigma_A^2 \omega_A^2 + \sigma_B^2 \omega_B^2 + 2\omega_A \omega_B \text{ COVAR}$$

Sharpe
 $\frac{B_A B_B}{\sigma_m^2}$

Markowitz
 $\sigma_A \sigma_B \gamma_{AB}$

↓
PART III
APT
(Multifactor Model)

$$ER = R_f + FRP_1 B_1 + FRP_2 B_2 \dots$$

↓
PART IV
PORTFOLIO
REBALANCING

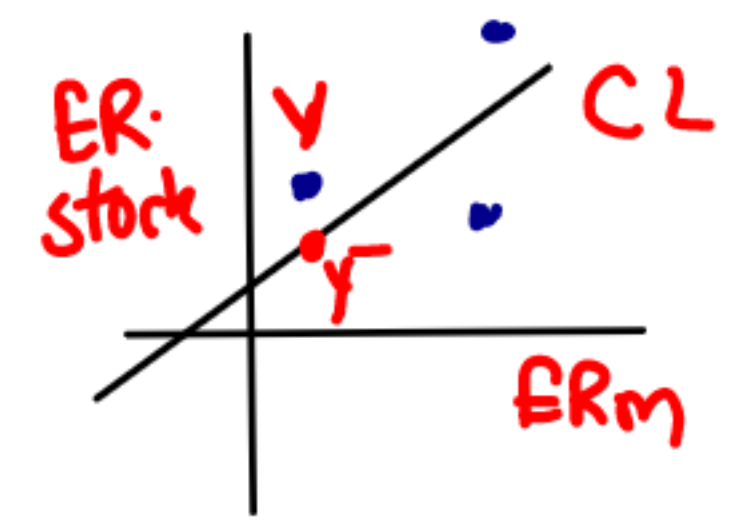
- ① Buy & Hold
- ② Constant Ratio
(Equal Amt of Bond & Equity)
- ③ CPP I
 $E = m(A - f)$

↓
PART V
Sharpe optimization
Model

- (i) Treynor Ratio = $\frac{ER - R_f}{\beta}$
- (ii) $C = \frac{\sigma_m^2 \times \sum \left(\frac{ER - R_f}{\sigma_{e_i}^2} \right) \beta}{1 + \left(\sigma_m^2 \sum \frac{\beta_i^2}{\sigma_{e_i}^2} \right)}$
Highest cutoff
- (iii) $Z_i = \frac{\beta}{\sigma_{e_i}^2} \left[\frac{ER - R_f}{\beta} - C \right]$

↓
Characteristic
Line

$$ER = \alpha + \beta R_m$$



Corner theory

$$y = a + b x$$

MUTUAL FUND

① NAV Calculation

Assets xxx
(-) Liabilities xxx
Net Asset xxx
÷ No. of Units xxx
NAV xxx

Entry Load / front End

$$POP = NAV + \text{Entry}$$

Exit Load / Back End Load

$$\text{Redemption} = NAV - \text{Exit}$$

$$\text{Expense Ratio} = \frac{\text{Exp. P.U.}}{NAV}$$

② Return Calculation

$$\bullet \text{ HPR} = \frac{\Delta \text{NAV} + \text{Dividend} + \text{Cap. Gain}}{\text{Beginning NAV}} \times 100$$

$$\bullet \text{ Annualised Return} = \text{HPR} \times \frac{12}{\text{period}}$$

• Indifference Return

$$R_2 = \frac{R_1}{1 - \text{Initial Exp.}} + \text{Recurring Exp.}$$

• Hedge fund

Basic fee = on AUM

Incentive fee = over Maximum Value

3 Performance Evaluation

$$1. \text{ Sharpe Ratio} = \frac{R_p - R_f}{\sigma}$$

$$2. \text{ Treynor's Ratio} = \frac{R_p - R_f}{\beta}$$

$$3. \text{ Jensen's Alpha}$$
$$\text{Alpha} = R_p - K_e$$
$$K_e = R_f + \beta(R_m - R_f)$$

Higher is better.

4 FAMA Model

• Return due to skill of Manager

$$\text{Return} = R_p - \text{CML}$$

• Return for compensation of UR

$$\text{Return} = \text{CML} - \text{SML}$$

5 Tracking Error

• Active Return = Actual Return - BM Return

• S.D. of Active Return = $\sqrt{\frac{\sum (x - \bar{x})^2}{n-1}}$ ← TR

• Information Ratio = $\frac{\text{Avg Active Return}}{TR}$

DERIVATIVES

PART I option

- Call option \rightarrow price Rise
- put option \rightarrow price fall
- European option \rightarrow on maturity
- American option \rightarrow Anytime

	ITM	ATM	OTM
Call	$S > E$	$S = E$	$S < E$
Put	$S < E$	$S = E$	$S > E$

- premium \rightarrow
 - \rightarrow Intrinsic Value
 - Call = $S - E, 0$
 - Put = $E - S, 0$
 - \rightarrow Time Value
 - premium - I. value

- Expected value of option = Gross payoff \times prob.

OPTION PRICING

• Binomial model

- ① Risk Neutral prob.

$$p = \frac{R - d}{u - d}$$

$$C_0 = \frac{CuP + Cd(1-p)}{R}$$

- ② Delta Hedging

$$\Delta_{\text{Call}} = \frac{C_1 - C_2}{S_1 - S_2}$$

$$C_0 = S_0 \times \Delta - \text{P.V. of CI}$$

• Put Call parity

$$S_0 + P_0 = C_0 + \text{P.V. of EP}$$

• Black Scholes model

$$d_1 = \frac{\ln \frac{S_0}{K} + (r + \frac{\sigma^2}{2})t}{\sigma \sqrt{t}}$$

$$d_2 = d_1 - \sigma \sqrt{t}$$

$$C_0 = S_0 \times N(d_1) - \frac{K}{e^{rt}} N(d_2)$$

$$P_0 = \frac{K}{e^{rt}} N(-d_2) - S_0 \times N(-d_1)$$

FUTURE

(i) margin

If initial margin is less than maintenance margin, then margin call upto initial

$$\text{Initial Margin} = \mu + \beta \sigma$$

(ii) future pricing

$$F = S_0(1+r) - D$$

$$F = S_0 \times e^{(r-r_f)t}$$

If Actual F & Theoretical F are not equal then possibility of arbitrage

(iii) Beta management

No. of Contracts

$$= \frac{V_p \times (B_T - B_F)}{F \times m \times B_F}$$

We take opposite position in Nifty for Hedging.

Commodity future

① future pricing

$$F = (S + PVSC - PVcy)(1+r)$$

② future Hedging

$$\text{Hedge Ratio} = \frac{\sigma_S}{\sigma_F} \times \rho$$

Amt in future

$$= \text{Exposure} \times \text{Hedge Ratio}$$

Short position

Interest Rate Risk Management

PART I FRA

① FRA for Hedgers

$$\text{Net Settlement Amt} = \frac{N(RR - FR) \frac{DTM}{Y}}{1 + (RR \times \frac{DTM}{Y})}$$

② FRA for ARBITRAGEUR

$$\text{Theoretical FRA} = \frac{\text{Bigger factor}}{\text{Smaller factor}}$$

- Actual FRA > Theoretical FRA
→ Sell FRA (Invest)
- Actual FRA < Theoretical FRA
→ Buy FRA (Borrow)

II IRG

- premium paid
- FRAPTION

III IRF

- Quotation = 100 - Rate
- Int Rate Rise = Sell future

IV Financial swap

(i) Plain Vanilla swap



② Overnight Index Swap

- MIBOR
- Daily compounding

③ Two party swap

V Cap, collar, Floor

(i) Cap

- Borrow
- Int Rate Rise

(ii) Floor

- Invest
- Int Rate fall

(iii) Collar

Buy cap & sell floor

FOREX

1. BASICS

- ₹/\$ 70 \$1000
- \$/₹ 0.0140 \$5000

Bid Ask Rates

₹/\$ 70.25/70.75
\$1000 Buy

₹/\$ 125/145
₹2000 Buy

Cross Rates

- ₹/\$ 60
- \$/£ 1.50 ₹/£
- ₹/£ 90
- \$/£ 1.50 ₹/\$
- ₹/\$ 70.25/70.75
- \$/£ 1.50/1.52
- ₹/£ = ?
- ₹/£ 90.45/91.25
- ₹/\$ 71.25/71.75
- \$/£ = ?

2. ARBITRAGE

₹/\$ 60.50 India
\$/£ 1.5045 USA
£/₹ 0.0125 UK
₹ 100000

3. Forward Cover

- Expected Loss
- Expected SR & SR
- Saving in Loss
- Expected SR & FR
- premium or disc.

$$\begin{aligned} \text{₹}/\$ &= \frac{F - S}{S} (\$) \\ &= \frac{S - F}{F} (\text{₹}) \end{aligned}$$

Swap points

10/15 plus in SR
15/10 less from SR

4 COVER DEAL

Bank covers from other Bank & calculate Gain/Loss

5 IRP & PPT

IRP Equation

$$\frac{F}{S} = \frac{1 + r_A}{1 + r_B}$$

PPP Equation

$$\frac{E_S}{S} = \frac{1 + i_A}{1 + i_B}$$

Covered IN Arbitrage

GR ₹/\$ = 60
FR ₹/\$ = 61.50
INH ₹ = 12%
\$ = 8%
Borrow ₹ 6000000 or \$100000

6. CURRENCY Exposure

- (i) Leading & Lagging
Immediate or delay
- (ii) MMC
Liability है तो Asset create
- (iii) FUTURE
जिस बात का डर, उसी में betting
- (iv) OPTION

Affraid of Rise - Call
Affraid of fall - put
premium - GR
uncovered - FR

7 Cancellation

- Opposite position
Rate of same date
- Early delivery & overdue FC
- Swap loss & Intt
Early Delivery
Bank recover & pay
overdue
Bank only recover

(8) Currency A/C

- Nostro A/C
- Nostro A/C
- position

9. Borrowing

Borrow वहाँ से करें, जहाँ cost कम रहे

10. Investment

Invest वहाँ करें जहाँ से CI ज्यादा आए

11. Cash Management

- Centralized
- Decentralized

12. Currency Swap

Drilldip Inc.

13. Economic Exposure

Transaction Exposure
• Currency fluctuation
Economic or operating
• price elasticity of demand
OMEGA Inc.

INTERNATIONAL FINANCIAL MANA.

PROJECT APPRAISAL

- HOME CURRENCY APPROACH
Convert FC into HC at
FR using IRP or PPP
& calculate NPV
- Foreign currency Approach
Disc. FC using k_0 of
FC.
Disc. Rate = $\left(\frac{1+k}{1+i}\right) 1+i$

GDR/ADR

- Gross Issue = $\frac{\text{Amt required}}{1 - \text{Issue Exp}}$
- Issue price of GDR
Issue price per share \times No. of shares
in \perp GDR
- No. of GDR = $\frac{\text{Gross Issue}}{\text{Issue price of GDR}}$
- Cost of GDR = $\frac{D_1}{P_0} + g$
 $P_0 = \text{Issue price of GDR} - \text{Issue Exp.}$

BOND VALUATION

1. Bond Pricing

$$I.V. = PV \text{ of Intt.} + PV \text{ of RV}$$

$$ZCB = PV \text{ of R.V.}$$

$$\text{perpetual bond} = \frac{\text{Coupon}}{\text{required yield}}$$

2. Bond yield

$$C.Y. = \frac{\text{Coupon}}{CMP} \times 100$$

$$YTM = \frac{I + \left(\frac{R.V. - P}{n}\right)}{\frac{RV + P}{2}} \times 100$$

IRR method

$$\text{Realised YTM} = MIRR$$

Dirty price & clean price

$$\text{Dirty price} = I.V. \text{ of Bond} \\ \text{Including Acc. Intt}$$

$$\text{clean price} = \text{Dirty} - \text{Acc. Intt.}$$

3. Bond Risk

$$(D)ED = \frac{P_2 - P_1}{2P_0 \Delta Y}$$

(ii) Macaulay Duration

$$D = \sum W \text{ of P.V. } \times \text{YEAR}$$

$$MD = \frac{D}{1 + YTM}$$

$$D \text{ of ZCB} = \text{Maturity}$$

$$D \text{ of perpetual} = \frac{1 + YTM}{YTM}$$

(iii) Convexity

$$C^* = \frac{P_2 + P_1 - 2P_0}{2 \times P_0 \times \Delta Y^2}$$

$$\text{Convexity} = C^* \times \Delta Y^2 \times 100$$

(iv) Bond Immunization

$$D \text{ of Assets} = D \text{ of Liabilities}$$

4. Convertible Bonds

$$\text{Straight value of Bond} \\ = P.V. \text{ of future Intt} + R.V.$$

$$\text{Stock Value of Bond} \\ = \text{Shares per Bond} \times \text{CMP share}$$

$$\text{Premium over straight value} \\ = \frac{\text{CMP} - S.V. \text{ of Bond} \times 100}{S.V. \text{ of Bond}}$$

$$\text{Percentage of downside risk} \\ = \frac{\text{CMP} - S.V. \text{ of Bond} \times 100}{\text{CMP}}$$

$$\text{Conversion parity price} \\ = \frac{\text{CMP of Bond}}{\text{No. of shares}}$$

$$\text{Favorable Income differential} \\ = \text{Intt per share} - \text{Dividend per share}$$

$$\text{Premium pay back period} \\ = \frac{\text{Parity price} - \text{CMP share}}{\text{Favorable Income differential}}$$

5. Option Embedded Bonds

- Bond Refunding
- NPV decision
- disc. at Jkd

6. Yield structure

if forward rate given

$$P.V. = \frac{CI}{(1+r)^1} + \frac{CI}{(1+r)(1+r)}$$

if yield is given

$$PV = \frac{CI}{(1+r)^1} + \frac{CI}{(1+r)^2}$$

EQUITY VALUATION

1 Value of share

Walter's Model

$$P_0 = \frac{D + (E - D) \frac{2}{k_e}}{k_e}$$

Dividend Growth Model

$$P_0 = \frac{D_1}{k_e - g}$$

Two stage dividend disc.

$$P_0 = \text{P.V. of Dividend (Abnormal growth)} + \text{P.V. of Terminal Value}$$

2 Right

$$\text{Ex Right price} = \frac{M \times N + S \times R}{N + R}$$

$$\text{Value of Right} = \text{Ex. Right price} - \text{Sub price}$$

$$\text{or } (M - P) N$$

SECURITY ANALYSIS

Exponential Moving Avg

EMA = previous EMA
+ (closing price - previous EMA)
x Exponential factor

$$\text{Exponential factor} = \frac{2}{n+1}$$

2. EMH

Test of WEAK FORM

Run Test

$$\mu_h = \frac{2n_1n_2}{n_1+n_2} + 1$$

n_1 = NO. of PLUS

n_2 = NO. of Minus

$$\sigma_h = \sqrt{\frac{(n_1-1)(n_2-2)}{n_1+n_2-1}}$$

$$df = n_1 + n_2 - 1$$

$$\text{limit} = \mu \pm t \sigma$$

Auto correlation Test

Find out correlation between 2 period & correlation should be "0"

CORPORATE VALUATION

1 EVA

NO PAT

EBIT(1-t)

EVA

NO PAT - C/E * WACC

2 Valuation of firm

FCFF

EBIT xxx

(-) TAX xxx

NO PAT xxx

(-) [C-E-Dep] xx

(-) Δ WC xx

FCFF xxx

Disc. at K_0 &

get V_F

$$V_E = V_F - V_D$$

3 GEARING OF BETA

Asset Beta of 2 similar firm should be same

$$\beta_A = \left(\beta_E \times \frac{E}{E+D} \right) + \left(\beta_D \times \frac{D}{E+D} \right)$$

if not given, assume

β_D is zero